Maths at Tarbiyyah Primary School



Fractions, decimals and percentages

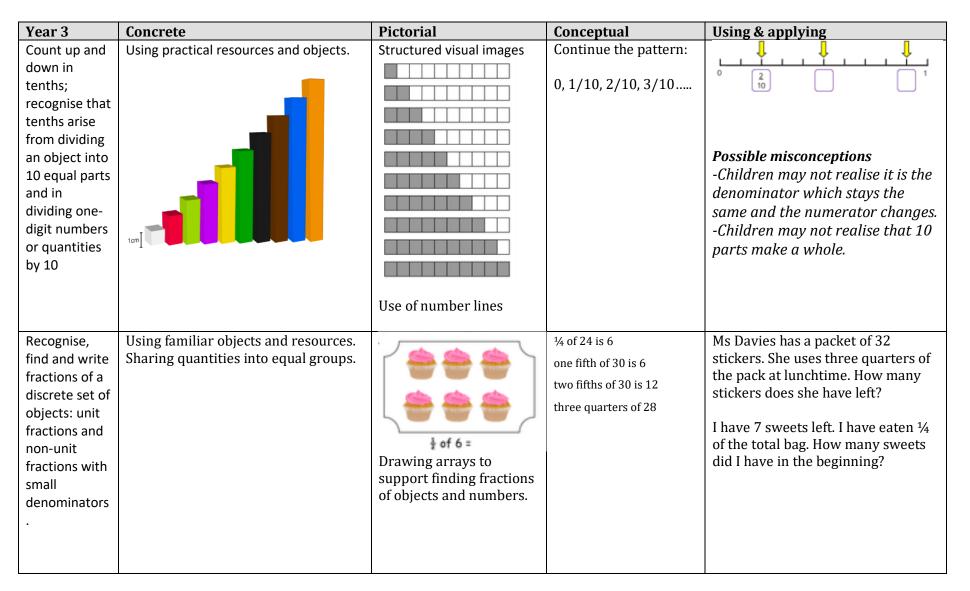
<u>EYFS</u>

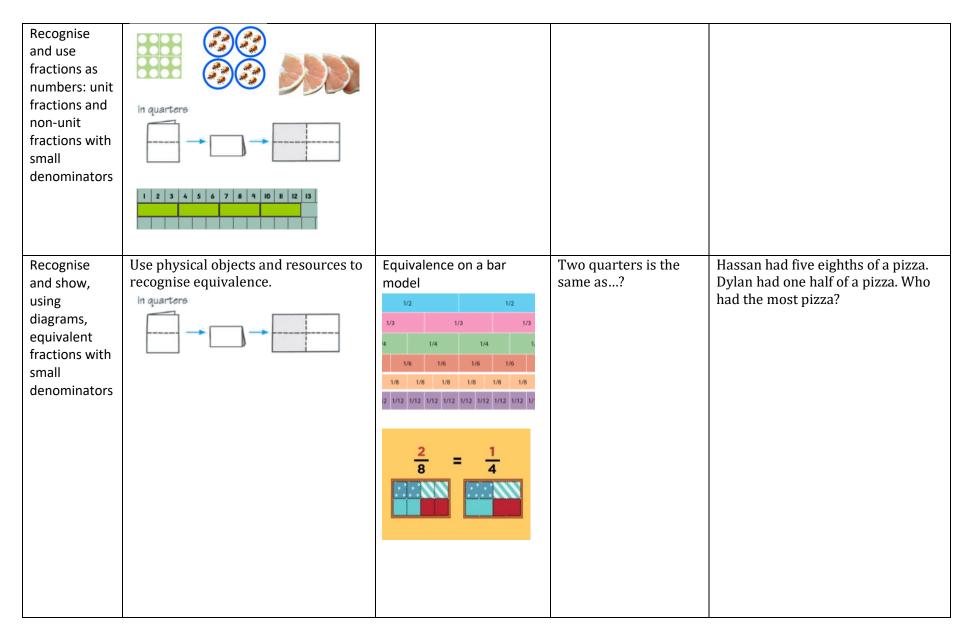
EYFS	Concrete	Pictorial	Conceptual	Using and applying
Solves	Using objects to show double.	Drawing pictures to show	Can I have half of	Discussions about sharing objects or
problems,		double and to half or 'share'.	your apple?	halving fruit.
including doubling, halving and sharing (ELG). (Numbers)	Using objects to show half and to share.	Laurente Transler Laurente Transler Laurente	Dubles Dubles 2 + 2 3 + 3 4 + 4 4 + 4	If Megan has 3 toys and Maheen has 3 toys, how many toys do they have altogether?
Year 1	Concrete	Pictorial	Conceptual	Using and applying
Recognise, find	Using familiar objects and	Using a variety of models	Recognise unit	I had 8 balloons.
and name a	resources.	and images	fraction notation:	I gave ¼ of them away.
half as one of	Sharing quantities into equal			How many balloons did I give away?
two equal	groups.		½ and ¼	How many do I have left?
parts of an				Use the numbers 1 to 20.
object, shape or quantity				Which numbers can you find ½ / ¼ of? What do you notice about your answers?
Recognise, find and name a quarter as one				
of four equal				

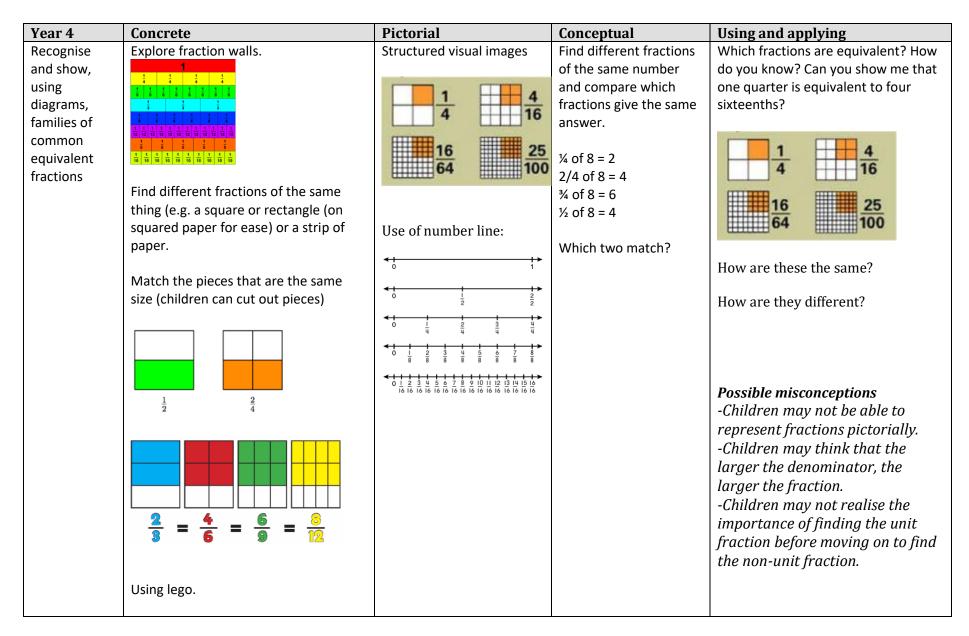
parts of an object, shape or quantity	in quarters 1 2 3 4 5 6 7 8 9 10 11 12 13 1 2 1 4 5 6 7 8 9 10 11 12 13			Possible misconceptions -Children may think that all parts do not need to be equal. - Children may think the bigger the denominator the bigger the part.
Year 2 Recognise, find, name and write	Concrete Using familiar objects and resources.	PictorialUsing a variety of modelsand images	Conceptual Recognise unit and non-unit fraction	Using and applying I had 20 balloons. I gave one two quarters of them away.
fractions one third , one quarter , 2 quarters and three quarters of a length, shape, set of objects or quantity.	Sharing quantities into equal groups.	V ₄ V ₂	notation: ¹ ⁄ ₂ and ¹ ⁄ ₄ 2 quarters, three quarters	How many balloons did I give away? How many do I have left? 2/4 is the same as? What other fractions are equivalent to 2/4?
	I 2 3 4 5 6 7 8 9 10 II 12 13			

Write simple fractions for example, half of 6 = 3 and recognise the equivalence of 2 quarters and one half.	Using familiar objects and resources. Sharing quantities into equal groups.	Sharing and grouping. E.g. one quarter of 8	Find fractions of quantities: ¹ / ₂ of 20 1/3 of 18 2 quarters of 24	 2/4 is the same as? What other fractions are equivalent to 2/4? Jacob had 24 sweets. He gave one third to his mum, one third to his dad and he kept one third for himself. How many did they have each? Alice, Adam and Maheen have ¾ of a cake. How much of the cake is left?
		One third of 12		Possible misconceptions -Children may think that all parts no not need to be equal. - Children may think the bigger the denominator the bigger the part. - Children may read fractions incorrectly e.g. thinking that ¼ is one part shaded, 4 parts not

Lower Key Stage 2:







	1 whole 1/2 C + + + + + + + + + + + + + + + + + +			-Children struggle to use different representations to show a fraction.
Recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten	Use Dienes equipment.	Place value chart.	1 ÷ 100 = 1/100 2 ÷ 100 = 2/100 3 ÷ 10 = 3/10 27 ÷ 100 = 27/100	What do you notice?1/10 of 100 = 101/100 of 100 = 202/100 of 100 = 2How can you use this to work out6/10 of 200?6/100 of 200?Possible misconceptions-Children may think that thelarger the denominator, thelarger the fractionChildren may not make therelationship between 1/10 and10/100.
	How many hundredths make one whole?			

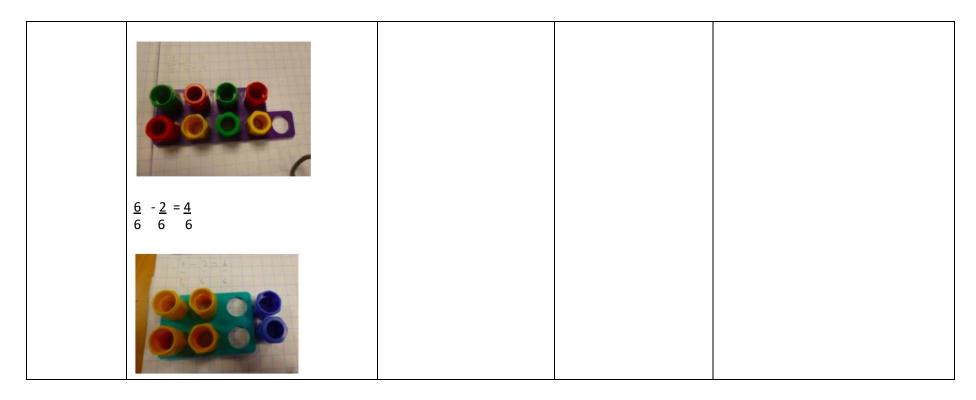
	Multilink can also be used where children physically break up the unit.			
Count up and down in hundredths.	Review counting in tenths before moving onto hundredths. Using the dienes rods, where 1 flat = 1 whole, 1 rod = 1 tenth. 1 unit = 1 hundred – children to physically move a unit piece and count in hundredth. Children to then recognise that 1 rod is the same as 10/100. If the start from 25/100 children to then add 1 unit rod whilst counting in hundredth. Use beads string to count up in 10 th and 100ths.	Structured visual images Use of number lines	Continue the pattern: 0, 22/100, 23/100, 24/100, 25/100 Count in hundredths from zero, then from any whole number, any hundredth and then any number (e.g. 2 and a half, 2 and 51 hundredths) Which is greatest: one tenth or one hundredth?	Spot the mistake sixty tenths, seventy tenths, eighty tenths, ninety tenths, twenty tenths and correct it. What comes next? 83/100, 82/100, 81/100,, Possible misconceptions -Children may not realise when counting up, denominator stays the same and the numerator changes. -Children may not realise that 100 parts make a whole. Children may not recognise that 1/10 is bigger than 1/100

Year 4	Concrete	Pictorial	Concentual	Using	anda	nalvin		
	Concrete		Conceptual		and a			
Recognise		$\begin{array}{c c} 1 & 1 \\ 0.10 & 100 \end{array}$		-		-	rn by filling in	tne
and write		0.10 100		blank			DIE:	
decimal		$0 \ 1 \ -1/10$		<u><u>1</u></u>	<u>2</u>	<u>3</u>		
equivalents of		$\begin{array}{rrr} 0.1 &= 1/10 \\ 0.2 &= 2/10 \end{array}$		10	10	10		
any number				<u>10</u>	<u>20</u>		<u>40</u>	
of tenths or		0.01=1/100		100	100		100	
hundredths.				0.1		0.3		
	One 0.1 0.01							
				 Another and another Write a decimal numbers (to one decimal place) which lies between a half and three quarters? and another, and another, Possible misconceptions Children may not recognise the bigger the denominator the smaller the parts. Children may think that 0.01 is bigger than 0.1.		а		

Recognise and write decimal equivalents to ¼,½,¾	Use a counting stick marked in divisions of 0.5 to familiarise children with counting forwards and backwards in steps of 0.5 (link to counting forwards and backwards in ½). What fraction does this present?	Use 10x10 grids and establish each square is one hundredth (0.01). Find fractions of the square (100) and use it to write decimal equivalents.	Continue the pattern – 0.25, 0.5, 0.75, 1, 1.25, 1.5 Counting on the counting stick in ¼ and 0.25. Missing numbers.	Ordering Put these numbers in the correct order, starting with the smallest. ¼ 0.75 5/10 Explain your thinking Possible misconceptions Children ½ is the same as 5/10 which is the same as 0.5. Children may not recognise that 0.25 is half of 0.5.
Compare numbers with the same number of decimal places up to two decimal places.	Help children become aware of the relative size of decimal numbers by ordering a set of amounts of money or lengths. f1.23 f1.03 f1.03 f1.03 f1.03	Position decimals on a number line for children to get a sense of size.	Put these numbers in descending order: 1.23, 1.03, 1.31, 1.32, 1.02 Include numbers to overcome misconceptions such as mistaking the length of the number with its size, for example thinking that 4.05 is larger than 4.5.	Missing symbol Put the correct symbol < or > in each box 3.03 3.33 0.37 0.32 What needs to be added to 3.23 to give 3.53? What needs to be added to 3.16 to give 3.2? Which is the larger amount, £0.75 or 90p? Which is longer, 3.06 m or 3.6 m? Which is larger: 239p or £2.93? Why? Possible misconceptions

				Children may think that 0.09 is bigger than 0.2 because '9' is larger than '2'.
Round decimals with one decimal place to the nearest whole number	Present children with a number line and digit cards (whole numbers).	Children to place digits on a number line, draw how many jumps to the whole numbers either side. $\frac{1}{0}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	 What is 4.7 rounded to the nearest whole number? I rounded my number to 3. What number (with one decimal place) could it have been? What is the biggest/smallest number I would round to 2? Simon rounded 1.6 to 2. Was he right? Explain how you know. Show me why I would round 2.3 to 2. My chair is nearly 1 m high. How tall could it be? Do, then explain Circle each decimal which when rounded to the nearest whole number is 5. 5.3 5.7 5.2 5.8 Explain your reasoning
				<i>Possible misconception</i> -Children may find the next multiple instead of the closest multiple.
Find the effect of dividing	Use place value grids.	ITP	Create numbers and look at effect of dividing by 10 and 100. Explore the visual	What is ÷ 10/÷ 100 ? How do you know? Can you show me? How to divide by ten? What mistake Have I made here?

a one- or two- digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths.	PLACE VALUE CHART	Use the Moving digits TP to model the effect of multiplying and dividing by 10, 100 and 1000.	pattern of the digits within division. 400 + 100 = 4 40 + 10 = 4 4 + 1 = 4 0.4 + 0.1 = 4 0.4 + 10 = 0.4 0.4 + 10 = 0.04	Possible misconceptions -Children may not be secure with what way to move the digits on the place value chart. -When dividing or multiplying a number with a 0 in between other digits i.e. 403, children may remove the 0.
Add and subtract fractions with the same denominator	Use fraction cards to model the $\begin{array}{c c} \hline 1 \\ \hline 4 \\ \\ \hline 7 \\ $	$\frac{1}{5} + \frac{2}{5} = \frac{3}{5}$ $\frac{1}{5}$ $\frac{1}{5}$ $\frac{1}{5}$ $\frac{2}{5}$ $\frac{1}{5} + \frac{2}{5} = \frac{3}{5}$ $\frac{6}{12} + \frac{3}{12} = \frac{9}{12}$ $\frac{6}{12} + \frac{3}{12} = \frac{9}{12}$	$\frac{1}{5} + \frac{2}{5} = \frac{3}{5}$ $\frac{6}{12} + \frac{3}{12} = \frac{9}{12}$ $\frac{12}{12} = \frac{12}{12}$	What do you notice? 5-1=4 5-5=5 4-1=3 5-5=5 Continue the pattern Possible misconceptions -Children may not be secure in understanding why the denominators doesn't change resulting in them adding or subtracting them.

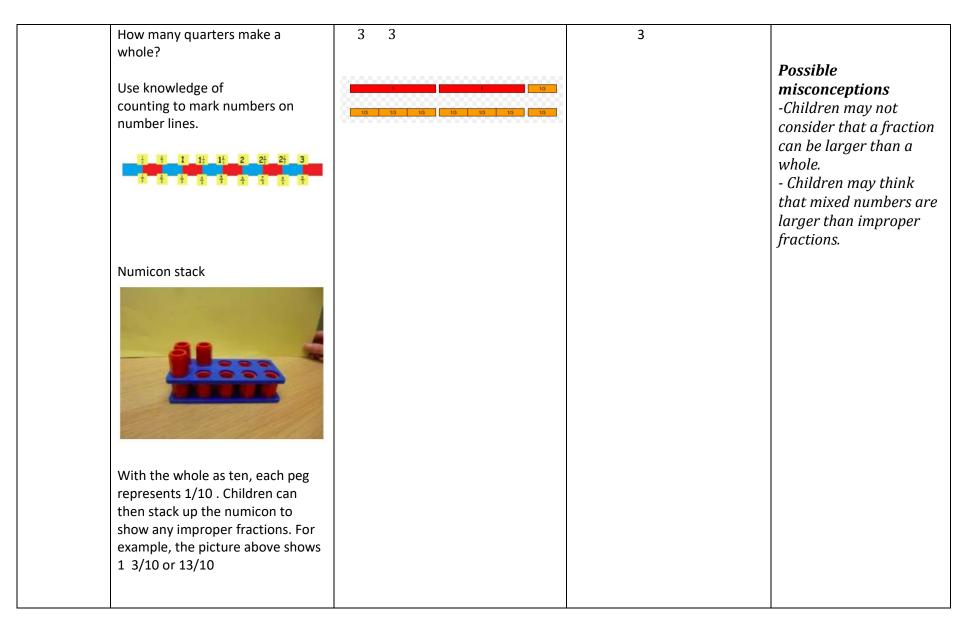


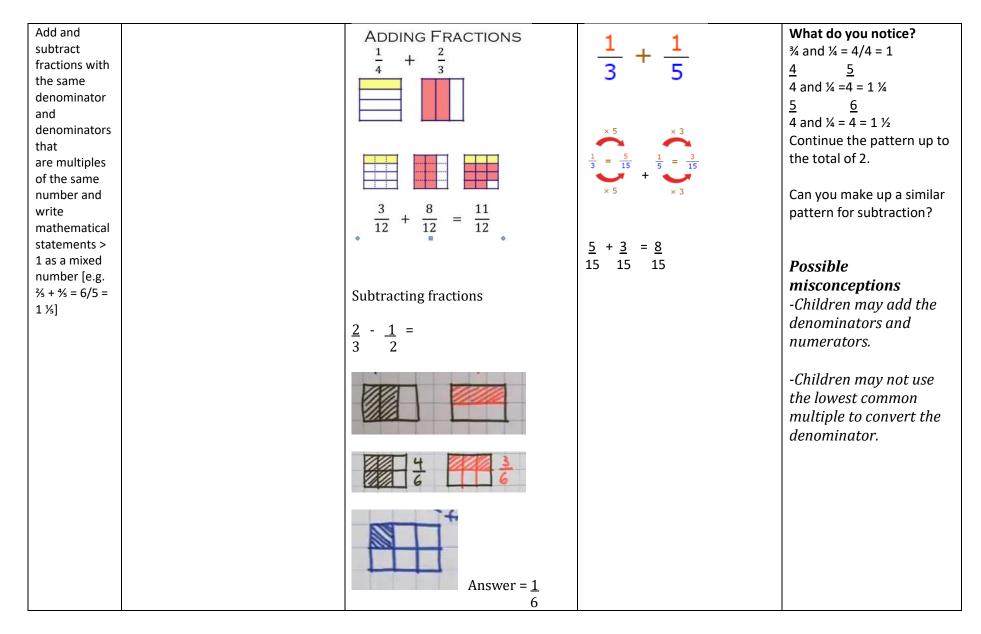
<u>Upper Key Stage 2:</u>

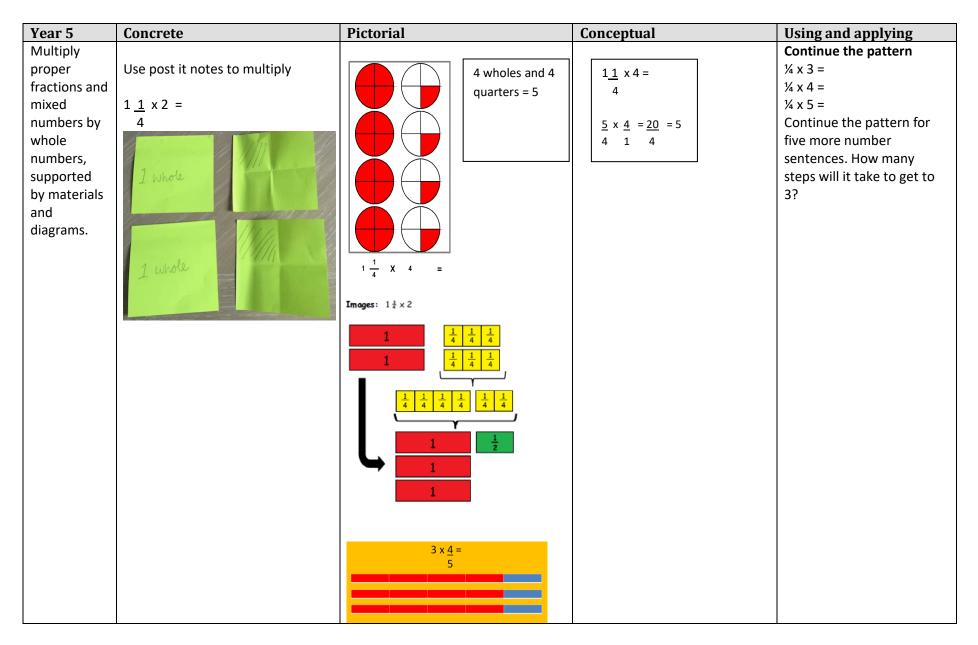
Year 5	Concrete	Pictorial	Conceptual	Using and applying
Compare and order fractions with denomina- tors that all have multiples of the same number.	Use fraction cards or a fraction wall to physically compare the sizes of fractions.	Draw objects which are the same size to compare. $\begin{array}{c c c c c c c c c c c c c c c c c c c $	Use knowledge of simplifying and finding a common denominator to compare fractions with denominators that all have multiples of the same number.	Give an example of a fraction that is more than three quarters. Now another example that no one else will think of. Explain how you know the fraction is more than three quarters. Possible misconceptions -Children may not be secure in finding equivalent fractions. Children may not find the lowest common denominator resulting in them working in efficiently.
Identify, name and write	Use various models and images to represent fractions in different ways.	Use of fraction wall to find equivalence	Investigate using multiplication and division to create equivalent fractions and to	Odd one out. Which is the odd one out in each of these collections of 4 fractions:

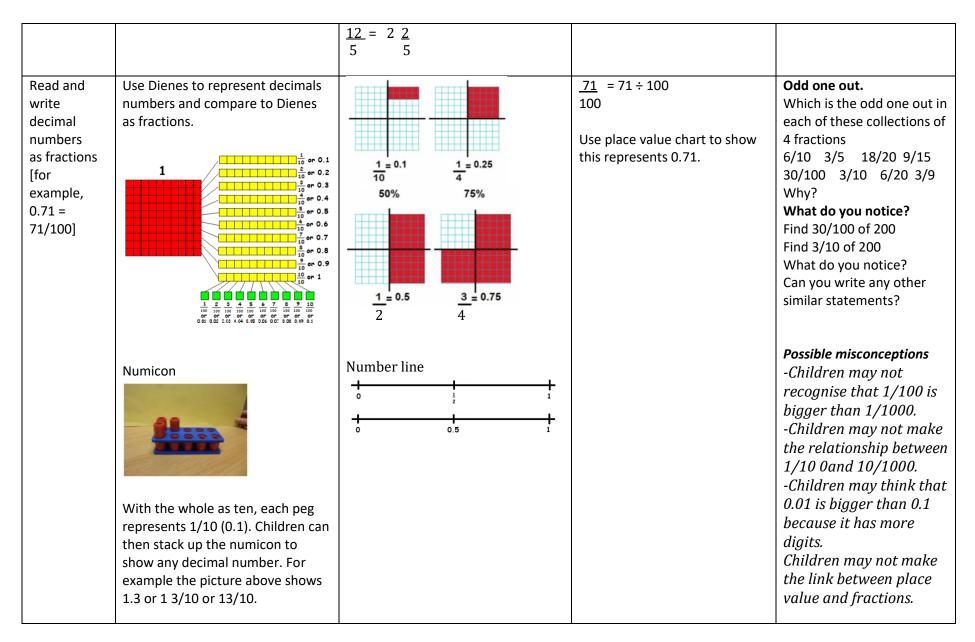
equivalent fractions of a given fraction, represented visually, including tenths and hundredths	State State <th< th=""><th>simplify fractions to find simplest equivalent.</th><th>$\begin{array}{cccccccccccccccccccccccccccccccccccc$</th></th<>	simplify fractions to find simplest equivalent.	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
			Possible misconceptions -Although children may be able to find equivalent fractions, they may not fully understand they represent the same the size of a given value – lots of practical example will support their understanding of equivalent fractions. -Children may struggle to recognise common multiples. -Children may struggle to visualise when two fractions are equivalent.

Year 5	Concrete	Pictorial	Conceptual	Using and applying
Recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents.	Blow up' dienes so 1 cube represents 1 whole, and therefore unit cubes represent one thousandths.	Th H T O T O 7 4 5 2 1 8 0.1 1 1 1 1 2 2 0.08 8 hundredths 2 2 0 0.1 1 tenths 2 2 0 0 4 hundreds 400 4 400 4 hundreds 7000 7 thousands	Symbols: 1 + 10, 1 + 100, 1 + 1000 $\frac{1}{10}$ $\frac{1}{100}$ $\frac{1}{1000}$ 3.652 = 'three point six five = three units, six tenths, 5 hundredths and 2 thousandths = 3652 thousandths	How would you read this number 1.234? What is the place value of each digit? How many units are there? How many tenths? How many hundredths? How many thousandths? Possible misconceptions -Children may not recognise that 1/100 is bigger than 1/1000. -Children may not make the relationship between 1/100 and 10/1000. -Children may think that 0.001 is bigger than 0.1 because it has more digits.
Recognise mixed numbers and improper fractions and convert from one form to the other.	1 or $\frac{1}{4}$ 1 $\frac{1}{4}$ or $\frac{5}{4}$ 1 $\frac{1}{2}$ or $\frac{1}{4}$ 2	How many quarters are there in 2 and $\frac{3}{4}$? $\underbrace{\frac{1}{4} \frac{1}{4}}_{\frac{1}{4}} \underbrace{\frac{1}{4} \frac{1}{4}} \underbrace{\frac{1}{4} \frac{1}{4$	$\frac{7}{3} = 2\frac{1}{3}$ How many groups of 3 are there in 7? What us the remainder? Or $7 \div 3 = 2 r \underline{1}$	Tell me a fraction that is bigger than 3. How else could we write it? Show me what eight thirds looks like. What is equivalent to it? How can you prove it?

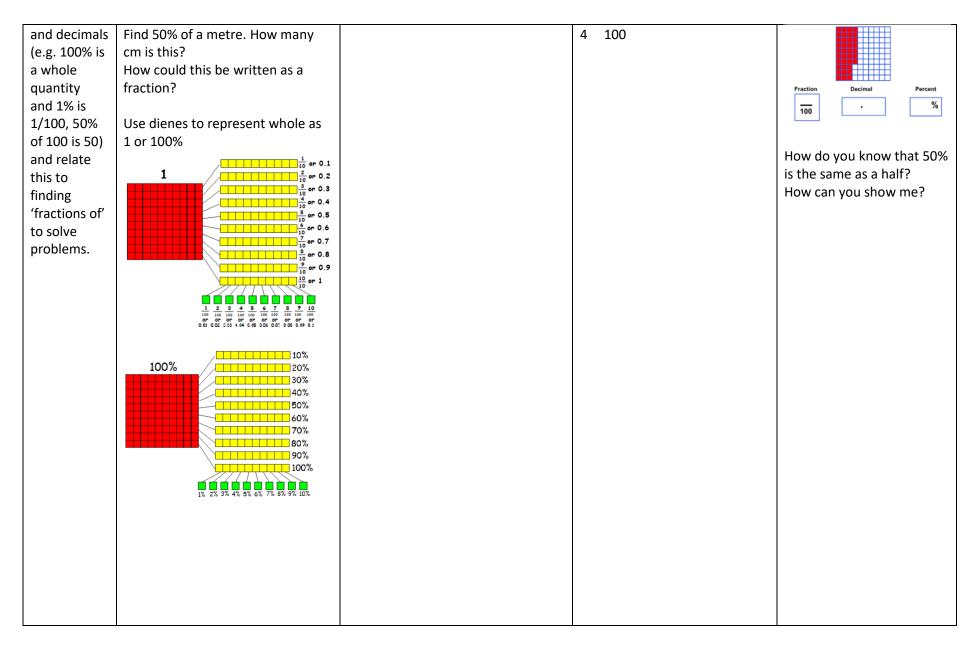








Recognise	Using the bead bar.	Represent percentage pictorially on	Percentage is a fraction out of	How can you model a
the per cent	Use the bead bar to discuss how	a 100 square.	100.	percentage?
symbol (%)	many 10% we can get out of 100%.			
and			$1\% = \frac{1}{100} = 0.01$	
understand	How many parts out of the 10		100	Ordering Put these numbers in the
that per cent relates to	does 10%/20%/30% represent?			correct order, starting with
feates to			70% = <u>70</u> = 0.7	the largest.
parts per	-		100	7/10, 0.73, 7/100, 0.073
hundred',		10% = 1		71%
and write		0.5		Explain your thinking
percentages		10		
as a fraction				Which is more:
with				20% of 200 or 25% of 180?
denominator	How can we write that as a			Explain your reasoning.
100, and as a	fraction?	1% = <u>1</u>		
decimal.	Using money.	100		Possible misconceptions
	Use money to show how 10p can	100		-Children may not make the link between
	be expressed as a percentage			
	and a fraction of £1. Give children			fractions percentages. -Children may not be
	the opportunity to use coins to	Images of everyday objects:		able to find equivalent
	convince themselves that, for			fractions to make the
	example, 10p is 1/10 or			denominator out of 100.
	10% of £1 because they need ten			
	10p coins to make £1.	$\frac{1}{2}$ = 50% = 0.5		
Understand	Counting stick to see the	Using a number line	Use equivalence to represent	Fill in the missing numbers
and use the	equivalence between the		fraction as part of 100.	in the
equivalence	numbers.		Use place value chart to show	Grid
between		0% 25% 50% 100%	how 25 ÷ 100 = 0.25	
percentages,		0 25cm 50cm 1m	4 25 250/ 2.25	
fractions			<u>1</u> = <u>25</u> = 25% = 0.25	



Year 6	Concrete	Pictorial	Conceptual	Using and applying
Use common	Numicon to find common factors.	Use fraction wall to show	Model dividing numerator and	What is the missing
factors to		equivalence of:	denomiator bu the same	number?
simplify fractions; use	$\frac{8}{12} = \frac{2}{3}$		number:	- —
common	12 3	$\frac{8}{12} = \frac{2}{2}$		
multiples to		12 3	$\frac{8}{100}$ (÷4) = 2	$\frac{10}{10} = \frac{10}{20}$
express			12 (÷4) 3	10 30
fractions in		1 whole		How do you know?
the same denomination		$\frac{1}{3}$ $\frac{1}{3}$ $\frac{1}{3}$		Tell me a fraction that is
denomination		$\frac{1}{4}$ $\frac{1}{4}$ $\frac{1}{4}$ $\frac{1}{4}$ $\frac{1}{4}$		equivalent to ½ but has a
		10 10 10 10 10 10 10 10 10 10 10 10 10 1		denominator of 9.
		$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		How did you do it?
		3 3		
		$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		Find the missing number:
				a 10
				3 _ 12
				□ [−] 16
				Karen makes a fraction
				using two number
				cards.
				She says,
				'My fraction is equivalent
				to $\frac{1}{2}$. One of the
				number cards is 6'
				Possible misconceptions
				-Children may not
				recognise the lowest
				common denominator.

Compare and order fractions, including fractions > 1	Using strips of paper: Which is greater 2 $\frac{4}{5}$ or 2 $\frac{3}{5}$? $5 \frac{1}{5}$ $\frac{1}{5}$ $$	Which is greater? 5 1 1 4 2 1 1 4 2	Find a common denominator: $\frac{5}{4}$ 1 $\frac{1}{2}$ = 1 $\frac{2}{4}$ 4 2 4 Convert both into a mixed number or improper fraction.	Give an example of a fraction that is greater than 1.1 and less than 1.5. Now another example that no one will think of. Explain how you know. Possible misconceptions -Children may not
				recognise that fraction can be more than one whole. -Children may think the larger the denominator, the larger the part. -Children may not recognise the lowest common denominator.
Add and subtract fractions with different denominator s and mixed numbers, using the	Use fraction wall cards : <u>11</u> - <u>1</u> = 12 3 11 - <u>1</u> = 12 3 10 + 1 + 1000 10 + 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 1000 10000 1000000000000000000000000000000000000	Bar modelling: $\frac{11}{12} - \frac{1}{3} = ?$ $\frac{1}{12} \frac{1}{12} \frac{1}{12}$ $- \frac{1}{3}$	$\frac{\frac{1}{3} + \frac{1}{5}}{\frac{1}{3} + \frac{5}{15}} + \frac{1}{5} + \frac{3}{15} + $	Of the flags in Jackie's Flag Shop, 3/5 are green and another 1/5 are teal. What fraction of the flags are either green or teal? Sadie's milkshake recipe needs 3/4 of a scoop of ice
concept of equivalent fractions		Find a common denominator:	$\frac{5}{5} + \frac{3}{15} = \frac{8}{15}$ 15 15 15	cream and Robbie's recipe needs for 1/4 of a scoop.

of proper fractions, writing the answer in its simplest form. $\frac{2 \times 1}{3} = \frac{2}{6}$ $\frac{2 \times 1}{3} = $			$\begin{array}{c} 1\frac{2}{3} + 2\frac{1}{2} \\ \text{Use denominators to draw grids (in this case 2 × 3) that represent units.} \\ \hline \\ $		How many more scoops of ice cream are used in Sadie's recipe than in Robbie's recipe?
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	simple pairs of proper fractions, writing the answer in its simplest	grids) to model the process of multiplying fractions.	use of 'of' in place of x. $ \frac{\frac{2}{5}}{\frac{x}{3}} \times \frac{\frac{2}{3}}{\frac{3}{3}} $ $ = \sqrt[3]{\frac{1}{2}} \times \frac{2}{\frac{1}{3}} + \frac{4}{15} $ $ \frac{1}{2} \times \frac{2}{5} = \frac{1}{2} \times \frac{2}{5} $	$\frac{1}{2} \times \frac{2}{5} = \frac{1 \times 2}{2 \times 5} = \frac{2}{10}$	the question (involving fractions / operations) Possible misconceptions -children may learn rule and not understand what the mathematics looks

